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## Design of a RISE Feedback Controller Tuned with PSO for 3DOF Robot Manipulator Trajectory Tracking

Marzieh Yazdanzad<sup>1\*</sup>, Alireza Khosravi<sup>1</sup>, Abolfazl Ranjbar Noei<sup>1</sup> and Pouria Sarhadi<sup>1</sup>

<sup>1</sup>Department of Electrical and Computer Engineering, Noshirvani University of Technology, Babol, Iran

\*Corresponding Author's E-mail: [s.yazdanzad@stu.nit.ac.ir](mailto:s.yazdanzad@stu.nit.ac.ir)

### Abstract

This paper presents an application of the recently proposed robust integral of the sign of the error (RISE) feedback control scheme for a three degrees-of-freedom (DOF) robot manipulator tracking problem. This method compensates for nonlinear disturbances and uncertainties in the dynamic model, and results in asymptotic trajectory tracking. To avoid selecting the parameters of the RISE controller by time-consuming trial and error method, particle swarm optimization (PSO) algorithm is employed as an intelligent technique. The objective of the PSO algorithm is to find the set of parameters that minimizes the mean of root squared error as its fitness function. The proposed method attains tracking goal, without any chattering in control input. Indeed, the existence of a unique integral sign term in the RISE controller avoids the occurrence of chattering phenomenon that usually happens in sliding mode controllers. Numerical simulations demonstrate the effectiveness of the proposed control scheme.

**Keywords:** Robust integral of the sign of the error (RISE), Asymptotic tracking, 3degrees-of-freedom robot manipulator, particle swarm optimization (PSO).

### 1. Introduction

In the past few decades, control of robotic systems has been studied significantly, because of their wide spectrum applications in medicine, aerospace, automotive and other industries. Robot manipulators are of highly nonlinear dynamic systems, which suffer from various



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uncertainties such as nonlinear friction, payload variation, unknown disturbances, and etc. Several control methods have been presented to attain an accurate tracking control of robot manipulators, such as adaptive control [1,2], sliding mode control [3,4], robust control [5] and neural network techniques [6,7].

Adaptive controllers can cope with the uncertainties in the dynamic model, and present fine tracking performance. However, this technique is restricted to compensate uncertainties which are linear in parameters. Sliding mode control is one of the effective strategies to control uncertain nonlinear systems. Main advantage of this method is strong robustness against system uncertainties, parameter variations and nonlinear disturbances [8]. But this technique, has some drawbacks including creating chattering phenomenon due to the discontinuous nature of control law, and the requirement of knowing an exact knowledge of the system dynamics [9].

It is difficult to obtain an exact mathematical model of robotic systems, due to modeling uncertainties, parameters variations, and etc. In recent years, intelligent control approaches such as neural network (NN)-based control and fuzzy control in robotic systems control, have received considerable attention [10,11,12]. Neural networks are almost able to approximate nonlinear continuous functions. They are therefore powerful tools to compensate for uncertainties, without knowing a complete knowledge of the plant [13]. Lewis et al. proposed a multilayer neural network controller for a robot manipulator which guarantees trajectory tracking performance [14]. However due to the NN functional reconstruction error, this type of controllers only achieve uniformly ultimately bounded (UUB) stability results. In order to eliminate the approximation error of NN-based controllers and achieving asymptotic tracking, Wai presented a sliding-mode neural network controller for rigid link manipulators [15]. In spite of obtaining asymptotic results, existence of a sign function in the robust term results in the destructive chattering phenomenon.



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Recently, a new feedback control strategy called robust integral of the sign of the error (RISE) is proposed in [16] which compensates for disturbances or uncertainties of dynamic system, by generating a continuous control signal [17,18]. In [19], Patre et al. utilized this method to develop a tracking controller in presence of additive disturbances and parametric uncertainties. The RISE method is a high gain feedback tool. Motivated by this issue, in [20, 21], a NN-based feedforward term is combined with the RISE feedback term in order to reduce the gain values of RISE feedback and to yield asymptotic tracking results. Also Shicheng Wang et al. in [22], designed a RISE based NN controller for a spacecraft formation within the leader follower architecture.

Particle swarm optimization (PSO) is a relatively new evolutionary computation technique inspired by the social behavior of birds flocking and fish schooling. It was first introduced by Kennedy and Eberhart in 1995 [23]. In fact, PSO is a population-based search method that can be used to find the optimal solution in a multidimensional search space. Optimization of the gains of a state feedback controller for a flexible manipulator, by PSO algorithm is presented in [24]. Also in [25], using PSO algorithm, an optimal design for a 6-DOF parallel manipulator has presented. Unlike other optimization methods, PSO gains from advantages such as simplicity of implementation and fast convergence.

In this paper, using the new RISE feedback control strategy, an asymptotic tracking is obtained for an uncertain nonlinear 3DOF rigid link robot system. PSO algorithm is applied to tune gains of the RISE controller by minimizing the root mean squared error of the robot. The obtained results represent satisfactory performance of the controller.

The remainder of this paper is organized as follows. First, in Section 2, nonlinear model of a 3 degrees of freedom robot manipulator is presented. Then, the RISE feedback control scheme is introduced in section 3. In section 4, PSO optimization technique is described. Simulation results for the 3DOF robot manipulator are provided in section 5, and eventually, conclusions are given in section 6.

## 2. Dynamics of Three Link Robot

The dynamics of a general rigid link manipulator having  $n$  degrees of freedom in free space, is as follows:

$$M(q)\ddot{q} + C(q, \dot{q})\dot{q} + G(q) + \tau_d = \tau \quad (1)$$

This dynamic equation is obtained by means of the Lagrangian approach. In equation (1) for the rigid 3DOF robot manipulator,  $q(t), \dot{q}(t), \ddot{q}(t) \in R^3$  are the position, velocity and acceleration of the joints, respectively.  $M(q) \in R^{3 \times 3}$  is the positive definite inertia matrix,  $C(q, \dot{q}) \in R^{3 \times 3}$  represents the Coriolis/centripetal matrix, and  $G(q) \in R^3$  expresses the gravity vector.  $\tau_d \in R^3$  denotes the vector of disturbances and un-modeled dynamics, and  $\tau \in R^3$  denotes the input torque vector applied to the joints. figure 1 shows the 3 link robot manipulator.

In this system the inertia matrix  $M(q)$ , the Coriolis/centripetal matrix  $C(q, \dot{q})$  and the gravity vector  $G(q)$  are as follows [26]:

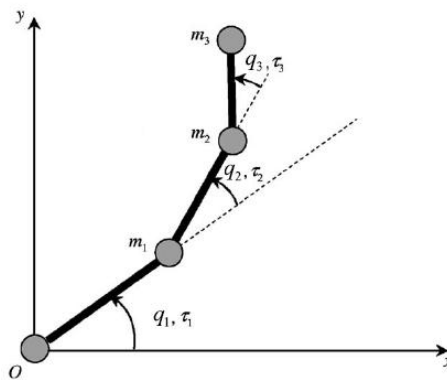


Figure 1: Three link planar robot



$$M(q, \dot{q}) = \begin{bmatrix} M_{11} & M_{12} & M_{13} \\ M_{21} & M_{22} & M_{23} \\ M_{31} & M_{32} & M_{33} \end{bmatrix}$$

with

$$\begin{aligned} M_{11} &= 2(d_1 + d_2 + d_3) + 2d_4c_2 + 2d_5c_{23} + 2d_6c_3 \\ M_{12} &= 2(d_2 + d_3) + d_4c_2 + d_5c_{23} + 2d_6c_3 \\ M_{13} &= 2d_3 + d_5c_{23} + d_6c_3 \\ M_{21} &= M_{12} \\ M_{22} &= 2(d_2 + d_3) + 2d_6c_3 \\ M_{23} &= 2d_3 + d_6c_3 \\ M_{31} &= M_{13}, \quad M_{32} = M_{23}, \quad M_{33} = 2d_3 \end{aligned}$$

and

$$C(q, \dot{q})\dot{q} = \begin{bmatrix} C_{11} & C_{12} & C_{13} \\ C_{21} & C_{22} & C_{23} \\ C_{31} & C_{32} & C_{33} \end{bmatrix} \begin{bmatrix} \dot{q}_1 \\ \dot{q}_2 \\ \dot{q}_3 \end{bmatrix}$$

where the  $C_{ij}$ , ( $i = 1,2,3$ ,  $j = 1,2,3$ ) are defined as follows:

$$\begin{aligned} C_{11} &= -\dot{q}_2d_4s_2 - d_5s_{23}(\dot{q}_2 + \dot{q}_3) - d_6s_3\dot{q}_3 \\ C_{12} &= -d_4s_2(\dot{q}_1 + \dot{q}_2) - d_5s_{23}(\dot{q}_1 + \dot{q}_2 + \dot{q}_3) - d_6s_3\dot{q}_3 \\ C_{13} &= -(d_5s_{23} + d_6s_3)(\dot{q}_1 + \dot{q}_2 + \dot{q}_3) \\ C_{21} &= (d_4s_2 + d_5s_{23})\dot{q}_1 - d_6s_3\dot{q}_3 \\ C_{22} &= -d_6s_3\dot{q}_3 \\ C_{23} &= -d_6s_3(\dot{q}_1 + \dot{q}_2 + \dot{q}_3) \\ C_{31} &= d_5s_{23}\dot{q}_1 + d_6s_3(\dot{q}_1 + \dot{q}_2) \\ C_{32} &= d_6s_3(\dot{q}_1 + \dot{q}_2), \quad C_{33} = 0 \end{aligned}$$

and

$$\begin{aligned} G(q) &= \begin{bmatrix} g_1 \\ g_2 \\ g_3 \end{bmatrix} \\ g_1 &= \frac{1}{2}a_1c_1m_1g + \left(a_1c_1 + \frac{1}{2}a_2c_{12}\right)m_2g + \left(a_1c_1 + a_2c_{12} + \frac{1}{2}a_3c_{123}\right)m_3g \\ g_2 &= \left(\frac{1}{2}a_2c_{12}\right)m_2g + \left(a_2c_{12} + \frac{1}{2}a_3c_{123}\right)m_3g \\ g_3 &= \left(\frac{1}{2}a_3c_{123}\right)m_3g \end{aligned} \tag{2}$$



where  $q = [q_1 \ q_2 \ q_3]^T$  and  $\dot{q} = [\dot{q}_1 \ \dot{q}_2 \ \dot{q}_3]^T$  contain the joints displacement and velocities, respectively.  $m_i$  and  $a_i$  are the masses and lengths of the joints. Meanwhile  $s_i, c_i, s_{ij}, c_{ij}, c_{ijk}$  ( $i = 1,2,3, j = 1,2,3, k = 1,2,3$ ) denote  $\sin(q_i), \cos(q_i), \sin(q_i + q_j), \cos(q_i + q_j), \cos(q_i + q_j + q_k)$ , respectively, and the parameters  $d_i, i=1, \dots, 6$  are defined as follows:

$$\begin{aligned} d_1 &= \frac{1}{2} \left[ \left( \frac{1}{4} m_1 + m_2 + m_3 \right) a_1^2 + I_{o1} \right] \\ d_2 &= \frac{1}{2} \left[ \left( \frac{1}{4} m_2 + m_3 \right) a_2^2 + I_{o2} \right] \\ d_3 &= \frac{1}{2} \left[ \left( \frac{1}{4} m_3 \right) a_3^2 + I_{o3} \right] \\ d_4 &= \left( \frac{1}{2} m_2 + m_3 \right) a_1 a_2 \\ d_5 &= \frac{1}{2} m_3 a_1 a_3 \\ d_6 &= \frac{1}{2} m_3 a_2 a_3 \end{aligned} \tag{3}$$

where  $I_{oi}, i = 1,2,3$  denotes the moment of inertia of  $i$ th joint [26].

It is assumed that  $q(t)$  and  $\dot{q}(t)$  are measurable and  $M(q), C(q, \dot{q}), G(q)$  and  $\tau_d(t)$  are unknown. Furthermore, the following properties for the dynamic model of the robot are hold:

**Property 1:** The inertia matrix  $M(q)$  is symmetric, positive definite and holds true the following inequality:

$$m_1 \|y\|^2 \leq y^T M(q) y \leq \bar{m}(q) \|y\|^2 \quad \forall y \in R^3 \tag{4}$$

where  $m_1 \in R$  is a known positive constant,  $\bar{m}(q) \in R$  is a known positive function and  $\| \cdot \|$  represents the standard Euclidean norm.

**Property 2:** If  $q(t), \dot{q}(t) \in \mathcal{L}_\infty$ , then  $C(q, \dot{q}), G(q)$  are bounded. Further, if  $q(t), \dot{q}(t) \in \mathcal{L}_\infty$ , then the first and second partial derivatives of the elements of  $M(q), C(q, \dot{q}), G(q)$  with



respect to  $q(t)$  exist and are bounded, and the first and second partial derivatives of the elements of  $C(q, \dot{q})$  with respect to  $\dot{q}(t)$  exist and are bounded as well.

**Property 3:** The nonlinear disturbance term and its first two time derivatives are bounded i.e.,  $\tau_d(t), \dot{\tau}_d(t), \ddot{\tau}_d(t) \in \mathcal{L}_\infty$ .

### 3. RISE Feedback Controller

Recently a novel feedback control scheme called robust integral of the sign of the error (RISE) is proposed in [16]. This method compensates for the disturbances or uncertainties of dynamic system using a continuous control signal. Using this technique, an asymptotic tracking is achieved without chattering problem that usually occurs in sliding mode controllers.

It is assumed that the desired trajectory,  $q_d(t) \in R^n$ , is designed such that  $q_d^{(i)}(t) \in \mathcal{L}_\infty, i = 1, 2, \dots, 5$ . In order to design a controller for the robot manipulator, with the aim of guaranteeing tracking of a desired time-varying trajectory,  $q_d(t) \in R^n$ , by the system, in spite of uncertainties and bounded disturbances in the dynamic model, a position tracking error, denoted by  $e_1(t) \in R^n$ , is defined as:

$$e_1 = q_d - q \tag{5}$$

The filtered tracking errors denoted by  $e_2(t), r(t) \in R^n$ , are also defined as:

$$e_2 = \dot{e}_1 + \alpha_1 e_1 \tag{6}$$

$$r = \dot{e}_2 + \alpha_2 e_2 \tag{7}$$

where  $\alpha_1 \in R^{n \times n}$  is a positive constant matrix and  $\alpha_2 \in R$  is a positive constant.

The continuous RISE feedback control law to attain the mentioned control objective is as follows [16]:

$$\tau(t) = (k_s + 1)e_2(t) - (k_s + 1)e_2(0) + \int_0^t [(k_s + 1)\alpha_2 e_2(\sigma) + \beta_1 \text{sgn}(e_2(\sigma))] d\sigma \tag{8}$$



where  $k_s, \beta_1 \in R$  are positive constant control gains and  $\text{sgn}(\cdot)$  is the standard sign function.

## 4. Particle Swarm Optimization Technique

### 4.1. PSO algorithm

PSO is a population-based optimization method inspired by the observation of social behavior of bird flocking. This method consists of a swarm of particles, where each particle represents a potential solution. In a PSO system, each particle flies through the multidimensional search space to adjust its position according to its own flying experience as well as the flying experience of its neighboring particle. In other word, each particle is considered as a point in search space, in which we try to find an optimal location.

Each particle  $i$  has a position vector  $X_i = (x_{i1}, x_{i2}, \dots, x_{iD})$ , and a velocity vector  $V_i = (v_{i1}, v_{i2}, \dots, v_{iD})$ , where  $D$  represents dimension of search space. Similar to the other optimization techniques, PSO requires a fitness function to evaluate performance of each particle. Further, each particle contains a memory to store the best position in the search space ever seen by it. Velocity and position are initialized with random vectors of the corresponding dimension. Trajectory of each particle in the search space is adjusted by updating it's velocity, according to the best position attained so far for it, denoted by  $pBest$ , and also the best position gained by any particle in the swarm, denoted by  $gBest$ , so far. The updating rule for the velocity and position of the  $i^{\text{th}}$  particle on dimension  $d$ , is as follows:

$$V_{id} = wv_{id} + c_1r_{1d}(pBest_{id} - x_{id}) + c_2r_{2d}(gBest_d - x_{id})$$

$$V_{id} = \begin{cases} V_d^{max} & , & v_{id} > V_d^{max} \\ -V_d^{max} & , & v_{id} < -V_d^{max} \end{cases}$$

$$x_{id} = x_{id} + v_{id} \tag{9}$$

where  $w$  is inertia weight that suitable selection of it provides a balance between local and global search ability.  $c_1$  And  $c_2$  are positive constants that represent the cognitive and social acceleration factors, respectively.  $r_{1d}$  and  $r_{2d}$  are two uniformly distributed random numbers





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in the range  $[0,1]$ .  $pBest_{id}$  denotes the position with the best fitness value, detected so far for the  $i^{\text{th}}$  particle.  $gBest$  Represents the best position obtained by the population. Furthermore  $V_{imax} = (v_{i1}^{max}, v_{i2}^{max}, \dots, v_{iD}^{max})$  represents an upper bound on the absolute amount of the velocity of the  $i^{\text{th}}$  particle. figure 2 indicates the flowchart of the PSO algorithm.

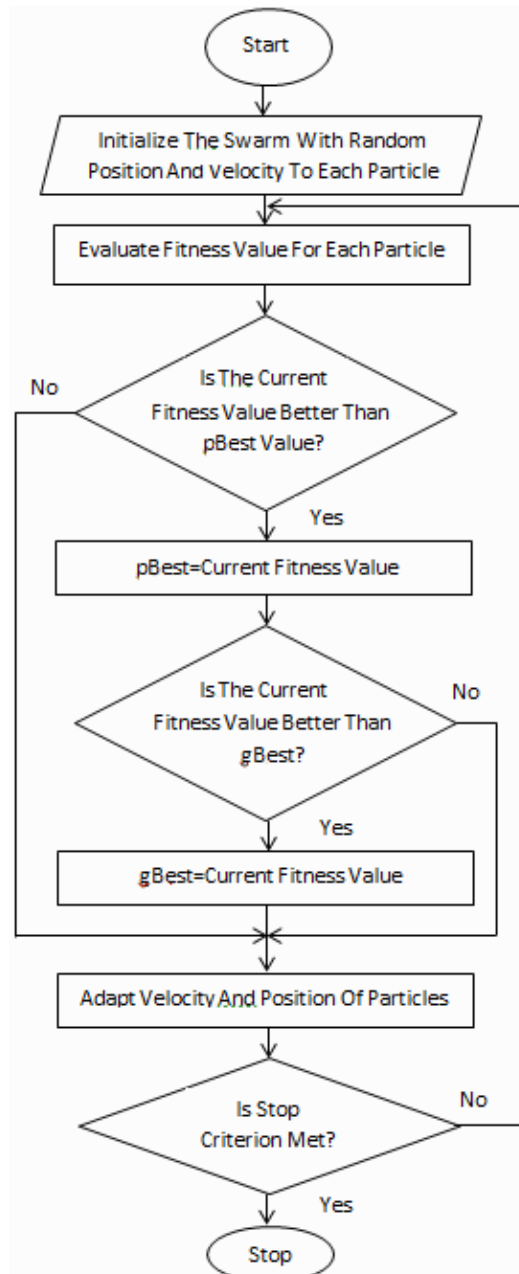


Figure 2. Flowcharts of particle swarm optimization algorithm [23]



4.2. Fitness function

In this section, PSO algorithm is applied to the RISE feedback controller for a three rigid link robot manipulator. The objective is to obtain the values of RISE controller gains,  $k_s, \beta_1, \alpha_2$ , by minimization of the objective function. In this paper, the mean of root of squared error is considered as the cost function, which for  $i^{th}$  particle is as follows:

$$MRSE = E(k) = \frac{1}{N} \sum_{i=1}^N \sqrt{e_{l1}^2(i) + e_{l2}^2(i) + e_{l3}^2(i)} \tag{10}$$

where  $e_{l1}(i), e_{l2}(i), e_{l3}(i)$ , are the trajectory tracking error of  $i^{th}$  sample for the first, second and third joint of the robot.  $N$  Is the number of samples and  $k$  is the iteration number.

5. Simulation Results

In this section, a numerical simulation for tracking control of a 3DOF rigid three link manipulator is performed to evaluate the validity of the proposed controller. By considering the robot system introduced in section 2, the numerical values of the robot are listed in TABLE I.

TABLE. 1: Simulation parameters of robot

	Mass ( $m_i$ , Kg)	Link ( $a_i$ , m)	Moment of inertia ( $I_{oi}$ , $Kgm^2$ )
Joint 1	1.2	0.5	$43.33 \times 10^{-3}$
Joint 2	1.5	0.4	$25.08 \times 10^{-3}$
Joint 3	3.0	0.3	$32.67 \times 10^{-3}$

The desired trajectory to be tracked by links is considered as  $q_d = [\sin(t), \cos(t), \sin(t + (\pi/3))]^T$ . Furthermore, external disturbances of  $\tau_{d1} = 0.2 \sin(2t), \tau_{d2} = 0.1 \cos(2t), \tau_{d3} = 0.1 \sin(2t)$  are applied to the system. Initial position



and velocity of the joints are set to zero. According to [27],  $\chi$  which is called the constriction factor, is defined as follows:

$$\chi = \frac{2}{\varphi - 2 + \sqrt{\varphi^2 - 4\varphi}}, \varphi = \varphi_1 + \varphi_2, \varphi > 4 \tag{11}$$

In PSO algorithm, the parameters  $\chi, \varphi_1, \varphi_2$  are set to 0.7298, 2.05, 2.05, respectively. The parameters  $w, c_1, c_2$  are defined according to the following equations:

$$w = \chi, c_1 = \chi\varphi_1, c_2 = \chi\varphi_2 \tag{12}$$

Gains of the RISE controller are continuously adjusted via PSO algorithm, to minimize the given objective function. Values of tuning parameters of the PSO algorithm are shown in TABLE II.

TABLE 2: PSO tuning parameters

Parameter	Value
Population Size	20
No. of Iterations (k)	50
	$v$ 3
	$w$ 0.7298
	$c_1$ 1.4962
	$c_2$ 1.4962
Lower Bound( $k_s, \beta_1, \alpha_2$ )	(0 0 0)
Upper Bound( $k_s, \beta_1, \alpha_2$ )	(30 30 30)

The achieved RISE feedback controller gains by the PSO algorithm, is given in TABLE III.

Table 3: Results of gains obtained

			Best Cost
25.32	16.7	29.3	0.001139

The simulation results are shown in figures 3 to 5.

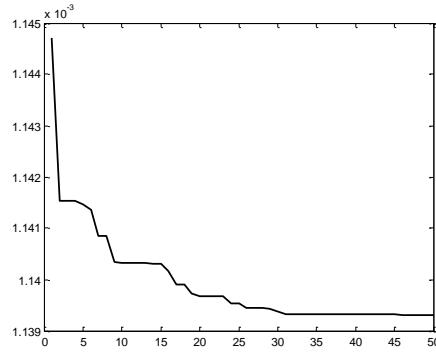
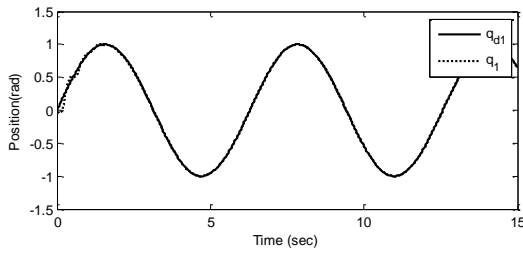
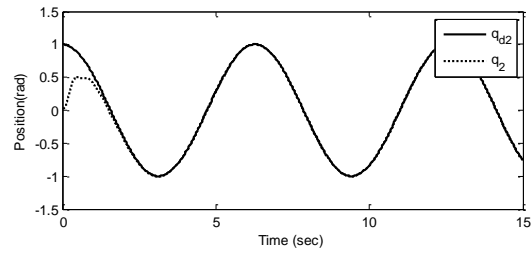


Figure 3: Fitness function values for 50 iterations

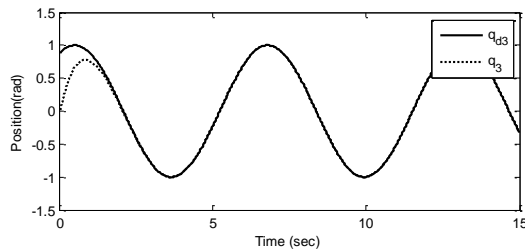
Figure 3 shows the fitness function trend, which is reduced to find the gain values of the RISE controller.



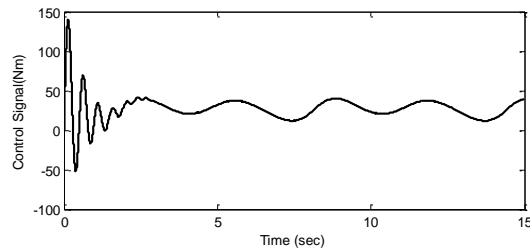
4. a. Trajectory tracking of joint angle 1



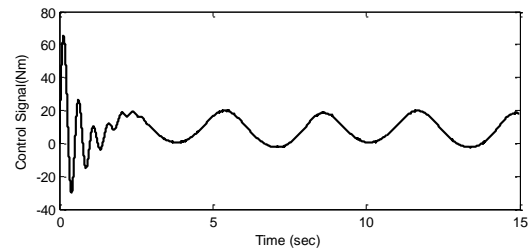
4. b. Trajectory tracking of joint angle 2



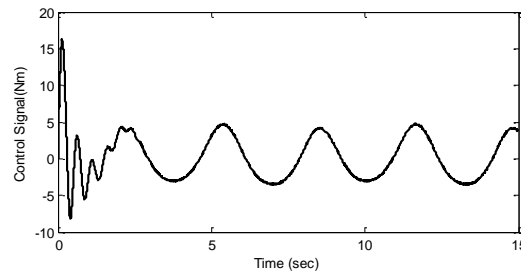
4. c. Trajectory tracking of joint angle 3



4. d. Control input for joint 1



4. e. Control input for joint 2



4. f. Control input for joint 3

Figure 4: Tracking position and control input of joints 1, 2 and 3

The trajectory tracking simulation results of all three joints of the robot and their corresponding control inputs applied to the system, are shown in figure 4. As it can be seen from the curves, the control objective is achieved successfully. Furthermore the proposed controller generates a continuous control signal, which prevents chattering phenomenon.

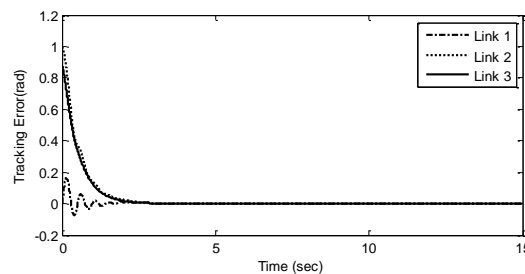


Figure 5: Tracking error of joints 1, 2 and 3



Figure 5 indicates the position tracking error for all three links of the robot, which confirms that asymptotic tracking is achieved even with the external disturbances.

## **Conclusion**

In this paper, a continuous control scheme called RISE feedback, has utilized for tracking problem of a 3 DOF rigid three link manipulator. An intelligent tuning of the RISE controller parameters is conducted by using particle swarm optimization algorithm. The controller parameters are adjusted while PSO minimizes the mean of root of squared error. The proposed controller compensates for uncertainties and bounded external disturbances without any chattering in control input. Simulation results have demonstrated the effectiveness of the proposed controller and its ability to provide an asymptotic tracking performance.

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